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1 **Numerical investigation of pressure and H₂O dilution effects on**
2 **NO formation and reduction pathways in pure hydrogen**
3 **MILD combustion**

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12 **Abstract**

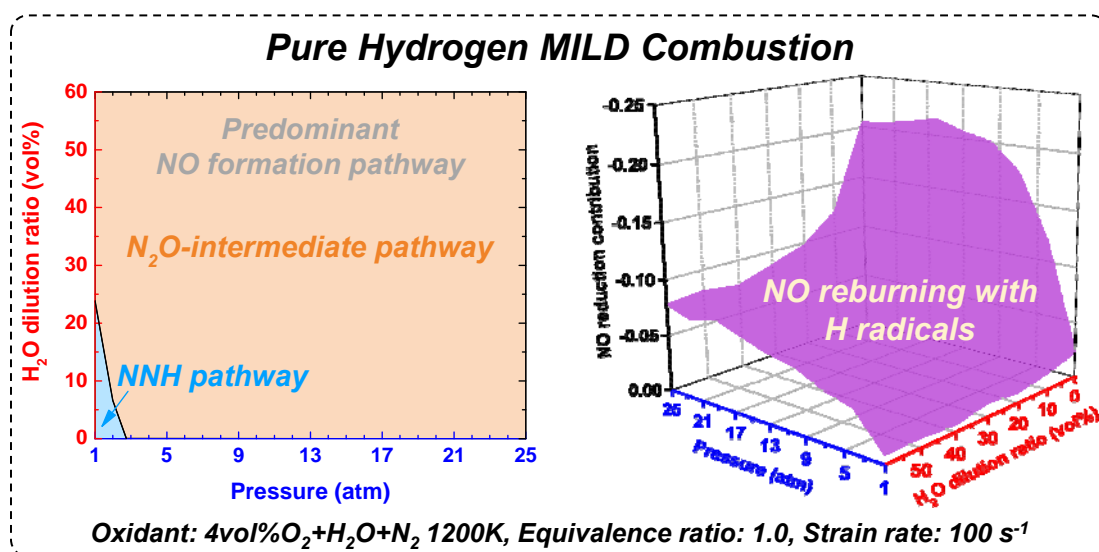
13 Pure hydrogen moderate or intense low-oxygen dilution (MILD) combustion offers a potential
14 solution to meet low NO emission needs while achieving rapid decarbonization for gas turbines. This
15 paper reports a numerical investigation of the pressure (1-25 atm) and H₂O dilution (0-60%vol,
16 including its physical and chemical effects) influences on NO formation and reduction pathways in
17 opposed-flow pure hydrogen diffusion MILD combustion, where the present NO sub-pathway analysis
18 method is also evaluated. Results show that, the present NO sub-pathway analysis method with
19 Glarborg2018 can respectively predict thermal NO, prompt NO, NO formed via NNH and N₂O-
20 intermediate, and NO reduced via CH_i and H reburning reasonably well. In pure hydrogen MILD

21 combustion, NO emission reaches its peak with the pressure up to about 6 atm due to more NO formed
 22 via N₂O-intermediate, and then decreases as the pressure is further raised, which is mainly attributed
 23 to less NO formation via NNH and more NO reduction by H radicals, finally causing the dominant
 24 NO formation pathway to transform from NNH to N₂O-intermediate at high pressure. The addition of
 25 H₂O, mainly because of its chemical effect to inhibit the NNH and N₂O-intermediate pathways via the
 26 channels NNH+O→NO and N₂O+H/O→NO, results in further NO emission reduction. The top NO
 27 contributor is changed from NNH to N₂O-intermediate with H₂O dilution at atmospheric pressure,
 28 while at high pressure, NO formation is invariably dominated by the N₂O-intermediate pathway even
 29 when H₂O is added up to 60%vol. NO reduction, which is initiated by the channel
 30 NO+H(+M)⇌HNO(+M), behaves more actively at high pressure, constituting 21% of the total NO
 31 produced at 25 atm, while its importance is weakened with H₂O dilution.

32 Keywords

33 MILD combustion, Opposed-flow flame, Hydrogen, Pressure, H₂O dilution, NO reaction pathway.

34 Graphical abstract



35

36 Nomenclature

Acronyms

MILD	Moderate or intense low-oxygen dilution
FLOX	Flameless oxidation
NG	Natural gas
OPPDIF	Opposed-flow diffusion flame
CRN	Chemical reactor network
ROP	Rate of production
JSR	Jet-stirred reactor
EINO	NO emission index

Symbols

FN_2	Factitious nitrogen
FH_2O	Factitious water vapor
P	Pressure
X_{O_2}	Oxygen volume fraction in the oxidant
X_{N_2}	Nitrogen volume fraction in the oxidant
$X_{\text{H}_2\text{O}}$	Water vapor volume fraction in the oxidant
X_{FN_2}	Factitious nitrogen volume fraction in the oxidant
$X_{\text{FH}_2\text{O}}$	Factitious water vapor volume fraction in the oxidant
U_f	Fuel injection velocity
T_f	Fuel temperature
U_o	Oxidant injection velocity
T_o	Oxidant temperature
T_{si}	Self-ignition temperature of reactants
a_s	Strain rate
L	Separation distance between two impinging nozzles

Greek letters

φ	Equivalence ratio
ρ_f	Fuel density
ρ_o	Oxidant density

38 **1. Introduction**

39 Rapid social-economic development accelerates the consumption of natural gas (NG) in gas
40 turbines, resulting in large emissions of carbon dioxide (CO₂) and further the greenhouse effect [1-3].
41 To mitigate this effect, hydrogen (H₂), which can be attained from water electrolysis powered by
42 renewable energy sources [4], has been considered as a promising zero-carbon alternative fuel to
43 natural gas for the decarbonized power supply with gas turbines [5]. However, pure hydrogen
44 combustion is prone to generate considerable amounts of nitrogen oxide (NO_x), mainly nitric oxide
45 (NO), because of its high flame temperature [6]. Thermoacoustic instability/oscillation may be also
46 encountered in gas turbines [7-12]. Hence, new clean and efficient hydrogen combustion technologies
47 need to be developed to promote source NO_x reduction while maintaining zero-carbon emissions
48 combined with good combustion stability for gas turbines.

49 Moderate or intense low-oxygen dilution (MILD) combustion [13], analogous to but not equal to
50 high temperature air combustion [14], flameless oxidation (FLOX) [15], and colorless distributed
51 combustion [16], is a promising low-NO_x combustion technology that can offer a potential solution to
52 achieve NO control/reduction during hydrogen combustion. Considering that reactants are highly
53 diluted by hot combustion products, MILD combustion is distributed throughout a furnace rather than
54 concentrated in a narrow flame front [15], featuring invisible flames, nearly-homogeneous temperature
55 fields, low thermoacoustic oscillations, and good combustion stability [14, 17]. Motivated by these
56 features, the MILD technology has been applied in furnaces [18] and is extending its application to
57 gas turbines [16, 17, 19-23].

58 Understanding the pressure effects on MILD combustion is mandatory if extending the MILD

59 technology to gas turbines. Using the FLOX[®] and COSTAIR burner technology, single-digit NO
60 emissions at atmospheric pressure have been demonstrated by Flamme [19] and Levy et al. [24]
61 reported that low NO emission levels can be also achieved if the pressure is elevated. Lückcrath et al.
62 [25] experimentally confirmed the applicability of the FLOX[®] burner to gas turbine combustors fueled
63 with NG/H₂ mixtures at 20 bar. In the FLOX[®] combustor, NO emission can be lower than 10
64 ppm@15%O₂ [26], which can be reduced by elevating the inlet velocity [25]. Huang et al. [27]
65 concluded that the pressure increase reduces OH mole fraction and subsequently causes the fuel
66 oxidation delay in syngas/hydrogen MILD combustion. Khalil and Gupta [28] experimentally
67 observed that as the pressure is increased (1-2.5 atm) at a constant inlet mass flow rate, NO emission
68 is increased inside a methane (CH₄) fueled MILD combustor. Besides higher NO emissions, a
69 departure from the MILD regime may occur with pressure elevation [23, 29-31]. Sadanandan et al.
70 [32] further reported hydrogen addition moves the reaction zone upstream with greater NO emissions
71 in the FLOX[®] combustor at 20 bar. Shi et al. [33] numerically concluded that NO emission from
72 opposed-flow syngas MILD combustion is reduced as the pressure increases from 1 to 20 atm, mainly
73 resulting from the decrease in NO formation via the NNH pathway.

74 **Table 1. Summary of the investigations on hydrogen-containing natural gas or syngas MILD**
75 **combustion at elevated pressure or/and H₂O dilution.**

Fuel	Oxidant	System	Method ^a	Pressure	NO factor studied	Mechanism	Reference
80/60%NG +20/40%H ₂	Air	FLOX [®] burner	EXP	20 bar	NO emission	/	[25]
60%NG+40 %H ₂	Air	FLOX [®] burner	EXP	20 bar	NO emission	/	[32]
48%CO+38	Air	CRN	SIM	1-19 atm	/	Davis	[27]

%H ₂ +14%C						mechanism	
O ₂ , H ₂							
CO/H ₂ (1:1)	O ₂ /N ₂ , O ₂ /H ₂ O/N ₂	OPPDIF	SIM	1-20 atm	NO formation	USC-Mech II +GRI-Mech 2.11's NO _x sub- model	[33]
H ₂	Air, O ₂ /N ₂ /H ₂ O	OPPDIF	SIM	1 atm	NO emission	GRI-Mech 3.0	[34]

^a EXP: Experiment, SIM: Simulation.

76 Increasingly stringent NO emission regulation forces to achieve further NO emission reduction
77 for hydrogen MILD combustion in gas turbines, where water (H₂O) injection is often used to control
78 NO formation [35]. Park et al. [34] numerically observed that the addition of H₂O to the air stream
79 decreases the flame temperature and hence suppresses NO emission in opposed-flow hydrogen/air
80 MILD combustion at atmospheric pressure with GRI-Mech 3.0. de Joannon et al. [36] found that steam
81 dilution significantly influences the reaction zone structures including temperatures and heat releases
82 in opposed-flow methane MILD combustion at 10 bar. Cheong et al. [37] noticed that H₂O addition
83 (0-15%) favors reducing the formation of NO from methane opposed-flow MILD combustion. Shu et
84 al. [38] numerically found that NO is formed mainly via N₂O in methane MILD combustion diluted
85 by H₂O. Si et al. [39] experimentally confirmed that H₂O dilution is more beneficial than N₂ dilution
86 for realizing natural gas MILD combustion, finally leading to lower NO emissions.

87 Emerging from the above literature review, the previous studies [25, 26, 28, 29, 32, 33] all targeted
88 natural gas and/or hydrogen-containing fuels in high-pressure MILD combustion (see Table 1),
89 whereas they were very less extended to pure hydrogen fuel at high pressure. Importantly, the NO
90 chemistry kinetic is heavily dependent on the hydrogen-blending ratio in MILD combustion [40].
91 However, during pure hydrogen MILD combustion at high pressure, especially over a wide range

92 covering the operating pressure of typical E-class and state-of-the-art H/J-class heavy-duty gas
93 turbines [41, 42], NO formation and reduction mechanisms were not addressed, especially including
94 NO reburning with H radicals that receives less attention despite hydrogen being capable to be used
95 as a reburn fuel to reduce NO [43], and the quantitative NO sub-pathway analysis method also needs
96 to be evaluated/validated based on experiments. In addition, how the reduction of NO proceeds during
97 pure hydrogen MILD combustion diluted by H₂O was not revealed, let alone the physical and chemical
98 effects of H₂O at different pressures with a recently-developed NO_x sub-model, which is required to
99 be investigated in order to achieve ultra-low and even near-zero NO emissions while maintaining zero
100 CO₂ production for gas turbines.

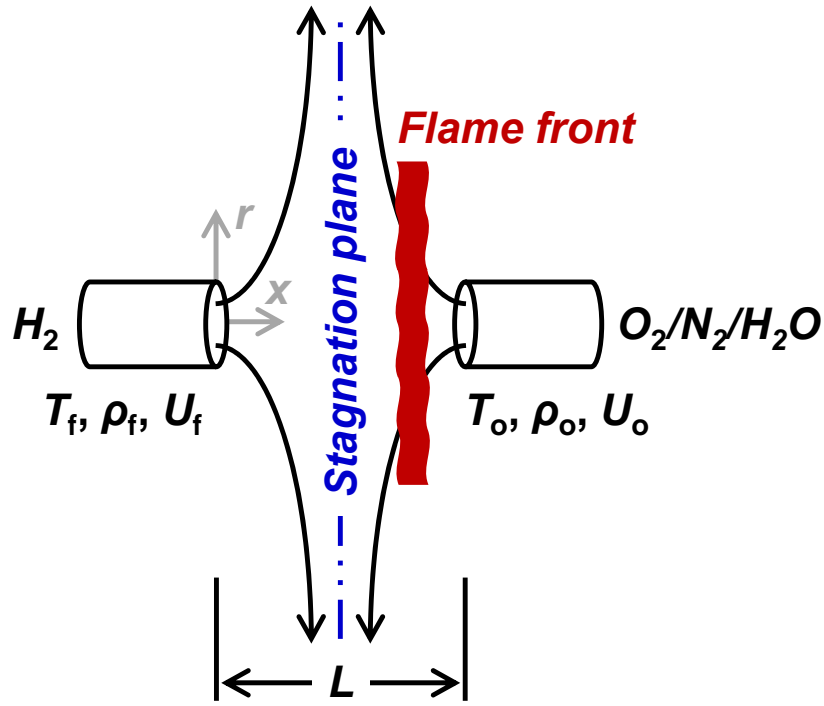
101 In this work, a computational parametric study using a detailed mechanism recently-proposed by
102 Glarborg et al. [44] in 2018 (termed Glarborg2018) is done to characterize the influence of pressure
103 (1-25 atm) and H₂O dilution (0-60%vol, including its physical and chemical effects) on NO formation
104 and reduction in opposed-flow pure hydrogen diffusion flames during MILD combustion. In particular,
105 the present NO sub-pathway analysis method coupled with Glarborg2018 for predicting NO formation
106 and reduction via six different pathways is evaluated, and then the quantitative NO reaction path
107 diagram analysis for pure hydrogen MILD combustion is performed, and NO formation via thermal,
108 NNH, and N₂O-intermediate pathways as well as NO reduction by H radicals are further investigated
109 at different pressure and H₂O dilution levels.

110 **2. Strategy of numerical modeling**

111 **2.1. Opposed-flow diffusion flames**

112 An opposed-flow diffusion flame (OPPDIF) stabilized in a steady, one-dimensional diffusive

113 layer, where a hot-diluted oxidant flow is employed to impinge on a room-temperature undiluted fuel
 114 flow, is used to model MILD combustion with the OPPDIF module in CHEMKIN [45]. The
 115 mathematical model used in this geometry has been described in the [Supplementary Material](#). As
 116 shown in [Figure 1](#), it consists of two opposed-flow nozzles separated by a finite distance (L), i.e., 1.5
 117 cm. Fuel and oxidant flows are injected through the nozzles with an inside diameter of 20 mm. Due to
 118 the impinging impact of these two flows, a stagnation plane is formed, whose location depends on the
 119 injection momentums of fuel and oxidant.



120

121 **Figure 1. Opposed-flow diffusion reactive configuration to model pure hydrogen MILD**
 122 **combustion.**

123 The strain rate (a_s) is defined as [46]:

$$a_s = \frac{2|u_o|}{L} \left[1 + \frac{|u_f|}{|u_o|} \sqrt{\frac{\rho_f}{\rho_o}} \right] \quad (1)$$

124 where ρ is density, u is gas flow velocity, and the subscripts “f” and “o” refer to fuel and oxidant,

125 respectively.

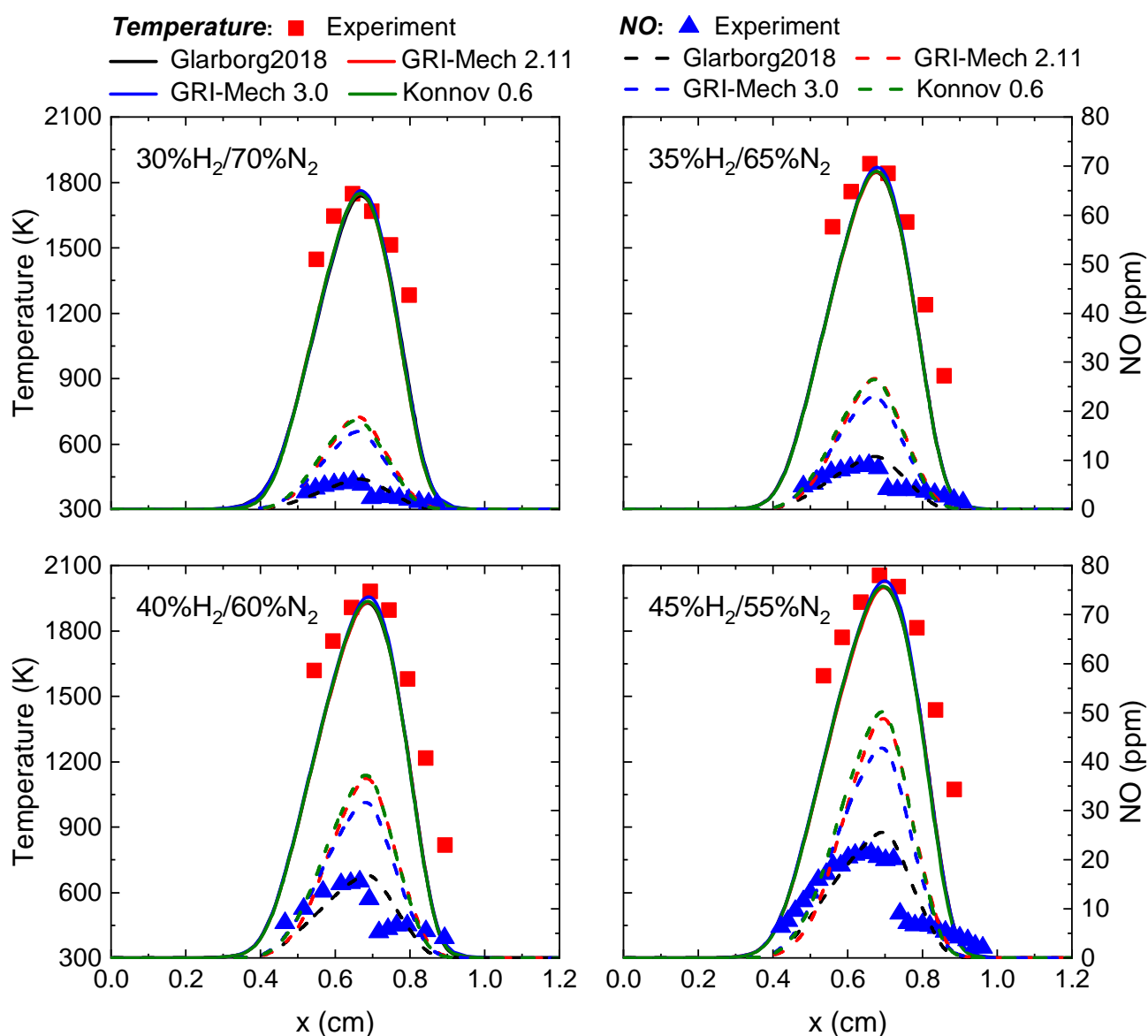
126 In the study, the opposed-flow flame calculations are performed by solving the gas energy
127 equation. Thermal diffusion and multicomponent transport are considered due to higher calculation
128 accuracy. To ensure converged solutions, adaptive mesh parameters GRAD and CURV are fixed at 0.1
129 and 0.5, respectively. Maximum number of grid points allowed is set as 350 to save computational cost
130 while ensuring solution accuracy. Absolute and relative tolerances are specified as 10^{-9} and 10^{-5} ,
131 respectively.

132 **2.2. Model validation**

133 Lots of reaction models have been developed for hydrogen and small hydrocarbon fuels, such as
134 GRI-Mech 2.11 [47], GRI-Mech 3.0 [48], Li mechanism [49], Davis mechanism [50], USC-Mech II
135 [51], Konnov 0.6 [52], and Glarborg2018 [44] often used. Among them, GRI-Mech is a classical and
136 widely-used reaction model for simulating the combustion of hydrocarbon and even hydrogen fuels
137 [34, 37, 38]. The models of Li et al. [49], Davis et al. [50], and USC-Mech II [51] were proposed for
138 hydrogen or hydrogen-containing fuels, while they lack NO_x chemistry. Konnov 0.6 [52] is applicable
139 to hydrogen/hydrocarbon fuels, including 129 species and 1231 reactions with nitrogen chemistry.
140 Glarborg2018 is a detailed reaction model recently-developed by Glarborg et al. [44], which consists
141 of 151 species and 1397 reactions with a detailed NO_x sub-model where the NNH/ N_2O reaction subsets
142 that are important, especially in hydrogen flames, have been updated.

143 In this study, the commonly-used kinetic mechanisms with nitrogen chemistry, i.e., GRI-Mech
144 2.11, GRI-Mech 3.0, Konnov 0.6, and Glarborg2018, are chosen for model validation. The ability of
145 these mechanisms to predict NO from pure hydrogen combustion is first validated against the

146 experimental data of Rørtveit et al. [53]. Figure 2 shows the predicted and measured temperature and
 147 NO mole fraction profiles in opposed-flow H₂/air diffusion flames at atmospheric pressure [53]. It is
 148 obvious in Figure 2 that the temperature profiles can be captured by all the reaction models with
 149 reasonable accuracy, whereas they perform very differently in NO prediction. In particular, the peak
 150 NO level is highly overestimated by GRI-Mech 2.11/3.0 as well as Konnov 0.6, while the NO predicted
 151 by Glarborg2018 is in better agreement with that observed experimentally in terms of its peak level
 152 and profile.



153

154

Figure 2. Measured [53] and predicted temperature and NO mole fraction in opposed-flow

H₂/air diffusion flames at atmospheric pressure.

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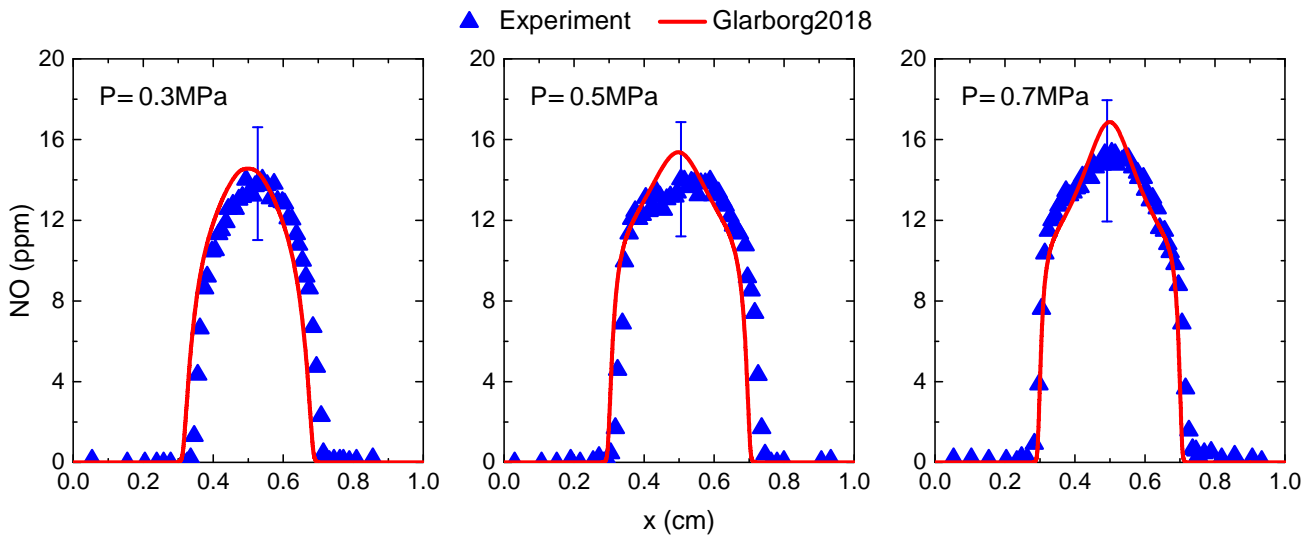
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To our best knowledge, there are no available experimental data of NO for opposed-flow H₂/air flames at high pressure. Accordingly, the experiment of high-pressure opposed-flow CH₄/H₂/air flames from de Persis et al. [54] is used to further check the Glarborg2018 predictability for NO at high pressure. Figure 3 plots the measured and predicted NO mole fraction profiles in opposed-flow CH₄/H₂/air flames at high pressure, which reveals that Glarborg2018 behaves reasonably well in the prediction of NO including its peak level and profile at elevated pressures up to 7 atm. Although the mechanism validation at high pressure is carried out based on a hydrogen-blending fuel rather than a pure hydrogen fuel, it can still demonstrate that Glarborg2018 has the predictive ability for hydrogen oxidation at high pressure, since the H₂/O₂ reaction subset is the fundamental kinetic in any hydrocarbon model.



166

167

168

Figure 3. Measured [54] and predicted NO mole fractions in opposed-flow CH₄/H₂/air flames with 20%vol hydrogen at high pressures.

169

170

As a whole, Glarborg2018 shows the best predictability for NO formation in hydrogen combustion at atmospheric and high pressures and therefore it is used in this study.

171 2.3. Operation parameters

172 Table 2 gives the operating conditions, where X_{O_2} , X_{N_2} , X_{H_2O} , X_{FN_2} , and X_{FH_2O} are the volume
 173 fraction of O_2 , N_2 , H_2O , FN_2 , and FH_2O in the oxidant, respectively. For all the cases studied, the
 174 fuel/air equivalence ratio (ϕ) at the nozzle inlet is maintained at 1.0 due to its significant effect on NO
 175 formation and reduction [40]. Hydrogen is fed as a fuel with a fixed injection velocity $U_f = 1.48$ cm/s
 176 at room temperature (i.e., fuel temperature (T_f) of 300 K), corresponding to Reynolds numbers of about
 177 27-670 at 1-25 atm, and oxygen diluted by N_2 and H_2O as the oxidant is introduced at a preheated
 178 oxidant temperature (T_o) of 1200 K with an injection velocity U_o equal to 74.21 cm/s corresponding to
 179 a strain rate (a_s) of 100 s^{-1} (following the study of Rørtveit et al. [53]). Note that all the cases in Table
 180 2 satisfy the definition of MILD combustion proposed by Cavaliere and de Joannon [13], where T_o is
 181 higher than the self-ignition temperature of reactants (T_{si}) but the temperature increase is lower than
 182 T_{si} , which indicates the occurrence of MILD combustion.

183 **Table 2. Cases investigated.**

	Fuel	Oxidant (vol%)					P (atm)	ϕ	U_f (cm/s)	U_o (cm/s)	a_s (s^{-1})
		X_{O_2}	X_{N_2}	X_{H_2O}	X_{FN_2}	X_{FH_2O}					
Series 1	H ₂	4	96				1-25	1.0	1.48	74.21	100
Series 2	H ₂	4	36-96	0-60			1	1.0	1.48	74.21	100
Series 3	H ₂	4	36-96		0-60		1	1.0	1.48	74.21	100
Series 4	H ₂	4	36-96			0-60	1	1.0	1.48	74.21	100
Series 5	H ₂	4	36-96	0-60			12	1.0	1.48	74.21	100
Series 6	H ₂	4	36-96		0-60		12	1.0	1.48	74.21	100
Series 7	H ₂	4	36-96			0-60	12	1.0	1.48	74.21	100

184 In this work, the pressure (P) is increased from 1 to 25 atm (covering the operating pressure of
185 typical E-class and state-of-the-art H/J-class gas turbines [41, 42]) to figure out the pressurized effects
186 on NO formation and reduction in pure hydrogen MILD combustion, corresponding to Series 1 in
187 Table 2. The H₂O mole fraction in the oxidant ($X_{\text{H}_2\text{O}}$) is varied from 0 to 60% at 1 and 12 atm (based
188 on the operating pressure of typical E-class gas turbines [41]) to examine the effect of H₂O dilution,
189 corresponding to Series 2 and 5 in Table 2. To further identify the physical and chemical effects of
190 H₂O, two artificial and chemically inert species, i.e., a fake nitrogen species (FN₂) and a fake water
191 species (FH₂O), are introduced. These two species have the same thermodynamical and transport
192 properties as N₂ and H₂O, respectively, but do not participate in reactions. Note that, the fake species
193 FN₂ is considered to eliminate the effect of the N₂ concentration decrease when H₂O is added to replace
194 N₂ in the oxidant. The differences between FH₂O and FN₂ are attributed to the physical effect of H₂O
195 due to the deviation of its physical properties from those of N₂. The differences between H₂O and
196 FH₂O addition are attributed to the chemical effect of H₂O. In Table 2, Series 3-4 and 6-7 are set to
197 grasp the physical and chemical effects of H₂O on NO formation and reduction pathways in pure
198 hydrogen MILD combustion.

199 **3. NO sub-pathway analysis method and its performance evaluation for** 200 **predicting the NO formed and reduced via different pathways**

201 **3.1. NO sub-pathway analysis method**

202 To examine the effect of each pathway on NO production separately, the NO sub-pathway analysis
203 method developed by Xu et al. [40, 55], which was first proposed for hydrogen-free fuels [55] and
204 then further extended to hydrogen-containing and/or pure hydrogen fuels [40], is adopted in this study.

205 As suggested in our recent works [40, 55], the key reaction subsets of thermal, prompt, NNH, and
 206 N₂O-intermediate mechanisms as well as NO reduction by hydrocarbon and non-hydrocarbon
 207 fragments for Glarborg2018 are categorized in Table 3, where the pathways of NO reburning with
 208 hydrocarbon fragments (e.g., C, CH, CH₂, CH₃, and HCCO) and non-hydrocarbon fragments (e.g., H)
 209 are referred to as CH_i reburning and H reburning, respectively.

210 **Table 3. Main reaction subsets for thermal, prompt, NNH, N₂O-intermediate, H reburning, and**
 211 **CH_i reburning pathways in Glarborg2018.**

Route	Reaction	No.	Reaction	No.	Reaction	No.
Thermal	N+NO \rightleftharpoons N ₂ +O	R674	N+O ₂ \rightleftharpoons NO+O	R673	N+OH \rightleftharpoons NO+H	R672
Prompt	CH+N ₂ \rightleftharpoons NCN+H	R944	CH+N ₂ \rightleftharpoons HNCN	R945	NCN+M \rightleftharpoons C+N ₂ +M	R1002
	CH ₃ +N \rightleftharpoons H ₂ CN+H	R925				
NNH	NNH \rightleftharpoons N ₂ +H	R675	NNH+O \rightleftharpoons N ₂ O+H	R677	NNH+O ₂ \rightleftharpoons N ₂ +HO ₂	R681
	NNH+O \rightleftharpoons N ₂ +OH	R678	NNH+O \rightleftharpoons NH+NO	R679		
N ₂ O- intermediate	N ₂ O+O \rightleftharpoons N ₂ +O ₂	R763	N ₂ O+O \rightleftharpoons NO+NO	R762	N ₂ O+H \rightleftharpoons N ₂ +OH	R761
	N ₂ O+OH \rightleftharpoons N ₂ +HO ₂	R764	N ₂ O(+M) \rightleftharpoons N ₂ +O(+M)	R760	NH+NO \rightleftharpoons N ₂ O+H	R667
H reburning	NO+H(+M) \rightleftharpoons HNO(+M)	R720				
CH _i reburning	CH ₃ +NO \rightleftharpoons HCN+H ₂ O	R930	CH ₃ +NO \rightleftharpoons H ₂ CN+OH	R931	CH ₂ +NO \rightleftharpoons HCNO+H	R937
	CH ₂ +NO \rightleftharpoons HCN+OH	R938	HCCO+NO \rightleftharpoons HCNO+CO	R997	HCCO+NO \rightleftharpoons HCN+CO ₂	R998
	CH ₂ (S)+NO \rightleftharpoons HCN+OH	R941	CH ₂ (S)+NO \rightleftharpoons CH ₂ +NO	R942	CH+NO \rightleftharpoons CO+NH	R948
	CH+NO \rightleftharpoons NCO+H	R949	CH+NO \rightleftharpoons HCN+O	R950	CH+NO \rightleftharpoons CN+OH	R951
	CH+NO \rightleftharpoons HCO+N	R952	C+NO \rightleftharpoons CN+O	R956	C+NO \rightleftharpoons CO+N	R957
	C ₂ H ₃ +NO \rightleftharpoons HCN+CH ₂ O	R979	C ₂ H+NO \rightleftharpoons HCN+CO	R985	C ₂ H+NO \rightleftharpoons CN+HCO	R986
	C ₂ +NO \rightleftharpoons C ₂ O+N	R989	C ₂ O+NO \rightleftharpoons CO+NCO	R1000	HCNO+H \rightleftharpoons HCN+OH	R866
	HCNO+O \rightleftharpoons HCO+NO	R867	HCNO+O \rightleftharpoons NCO+OH	R868	HCNO+OH \rightleftharpoons CO+H ₂ NO	R869
	HCNO+OH \rightleftharpoons HCO+HNO	R870				

212 Five simulations need to be done for each hydrogen flame to estimate the relative importance of
 213 each pathway, as presented in Table 4. In the first simulation (SIM1), the full mechanism is used, while
 214 the second (SIM2), third (SIM3), and fourth (SIM4) simulations are done using the full mechanism

215 without the initiation reactions of the H reburning pathway, without the initiation reactions of the H
 216 reburning and NNH pathways, without the initiation reactions of the H reburning, NNH, and N₂O-
 217 intermediate routes, respectively. The NO contributed by the H reburning, NNH, and N₂O-intermediate
 218 pathways is acquired by differentiating SIM1 with SIM2, SIM2 with SIM3, and SIM3 with SIM4,
 219 respectively. Thermal NO is predicted by the fifth simulation (SIM5) using the full mechanism with
 220 the NO_x sub-model only involving the three key reactions of thermal NO. Due to the absence of
 221 hydrocarbon species, the sub-mechanisms of prompt NO and CH_i reburning are disabled and thus
 222 omitted in the NO pathway analysis for pure hydrogen-firing cases.

223 **Table 4. Model processing procedure for pure hydrogen fuel.**

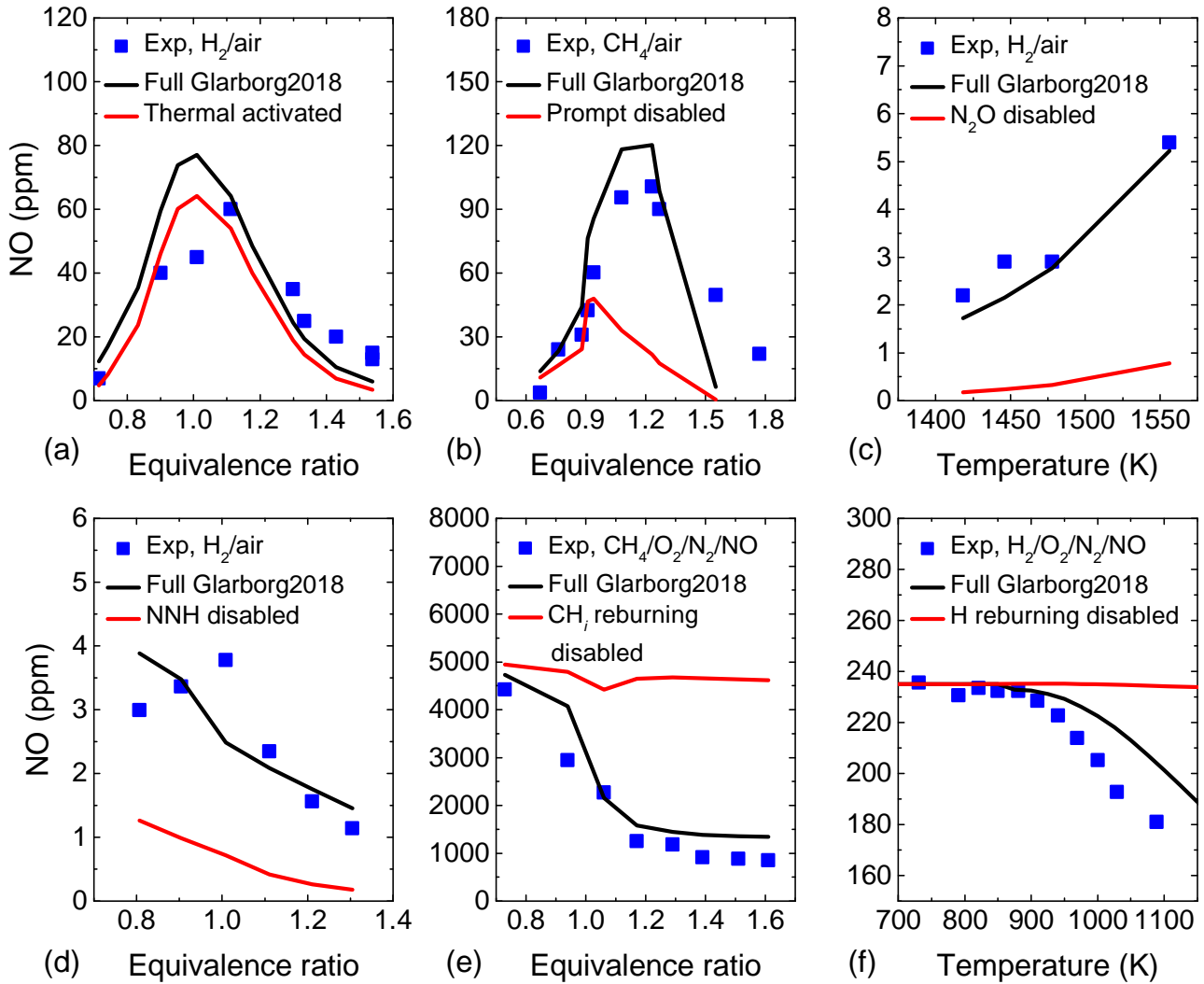
Model processing procedure	
SIM1	Full mechanism
SIM2	Deleting the initiation reaction of the H reburning pathway
SIM3	Deleting the initiation reactions of the H reburning and NNH pathways
SIM4	Deleting the initiation reactions of the H reburning, NNH, and N ₂ O-intermediate pathways
SIM5	Only remaining the initiation reactions of the thermal-NO pathway

224

225 **3.2. Performance evaluation of the NO sub-pathway analysis method**

226 To ensure the validity of the NO pathway analysis, the present NO sub-pathway analysis method
 227 with Glarborg2018 needs to be systematically evaluated for predicting the NO formed/reduced via the
 228 thermal, prompt, N₂O-intermediate, NNH, as well as CH_i and H reburning pathways, respectively. To
 229 this end, we choose the experimental data of NO from CH₄ or H₂ combustion [56-61] obtained under
 230 special conditions that favor NO formation via one of the above six pathways each time. [Figure 4\(a\)-](#)

231 (f) plots the predicted NO concentrations using the full Glarborg2018 mechanism with or without the
 232 initiation reactions (see Table 3) for one of the above six pathways against the experimental data [56-
 233 61].



234
 235 **Figure 4. Performance evaluation of the NO sub-pathway analysis method with Glarborg2018**
 236 **for predicting the NO formed/reduced via different pathways against the experimental data**
 237 **[56-61]: (a) Thermal-NO, (b) Prompt-NO, (c) N₂O-intermediate, (d) NNH, (e) CH_i reburning,**
 238 **(f) H reburning.**

239 **3.2.1. Thermal-NO**

240 Thermal-NO mechanism often dominates NO formation in high-temperature combustion
241 typically above 1800 K [62]. Figure 4(a) shows the measured [56] and predicted NO from H₂/air
242 combustion in a jet-stirred reactor (JSR) at 1830-2210 K, where if only the thermal-NO initiation
243 reactions are activated, NO is still predicted without a large decrement. NO is also contributed from
244 N₂O-intermediate/NNH under fuel-lean/fuel-rich conditions, which is responsible for the difference
245 between both models.

246 **3.2.2. Prompt-NO**

247 The JSR measurements of NO from CH₄/air combustion at $\phi=0.6-1.8$ [57] are compared in Figure
248 4(b) to check the prompt-NO prediction. It is found that if the prompt-NO initiation reactions are
249 removed from Glarborg2018, NO is still predicted well under fuel-lean conditions but highly
250 underestimated under stoichiometric/rich conditions, since prompt NO is the major NO source in
251 stoichiometric/rich conditions [44].

252 **3.2.3. N₂O-intermediate**

253 The JSR experimental data of NO from lean H₂/air combustion ($\phi=0.6-0.7$) at 1400-1550 K [58],
254 where NO is formed mainly via the N₂O-intermediate mechanism, is used. Figure 4(c) shows that if
255 the N₂O-intermediate initiation reactions are deleted from Glarborg2018, NO is severely
256 underpredicted and close to zero at low temperatures. Thermal NO is responsible for the phenomenon
257 where a small amount of NO is still predicted at higher temperatures without the N₂O-intermediate
258 mechanism.

259 **3.2.4. NNH**

260 Due to the predominant role of the NNH mechanism in forming NO at low-temperature and rich
261 conditions [63], the experimental NO data of H₂/air combustion at 1635 K and $\varphi=0.8-1.3$ from Purohit
262 et al. [59] are compared in Figure 4(d). When the NNH initiation reactions are disabled from
263 Glarborg2018, NO is found still emitted under fuel-lean conditions but notably underpredicted under
264 reducing conditions, especially for rich mixtures.

265 **3.2.5. CH_i reburning**

266 To evaluate the prediction performance of NO reduction by hydrocarbon fragments, Figure 4(e)
267 shows the comparison of the measured NO from combustion of CH₄ doped with 5000 ppm NO at 1580
268 K in a JSR [60] with the predictions. It is found that NO does not be reduced and is close to 5000 ppm
269 over the whole φ range when the CH_i reburning reaction subsets is disabled in Glarborg2018.

270 **3.2.6. H reburning**

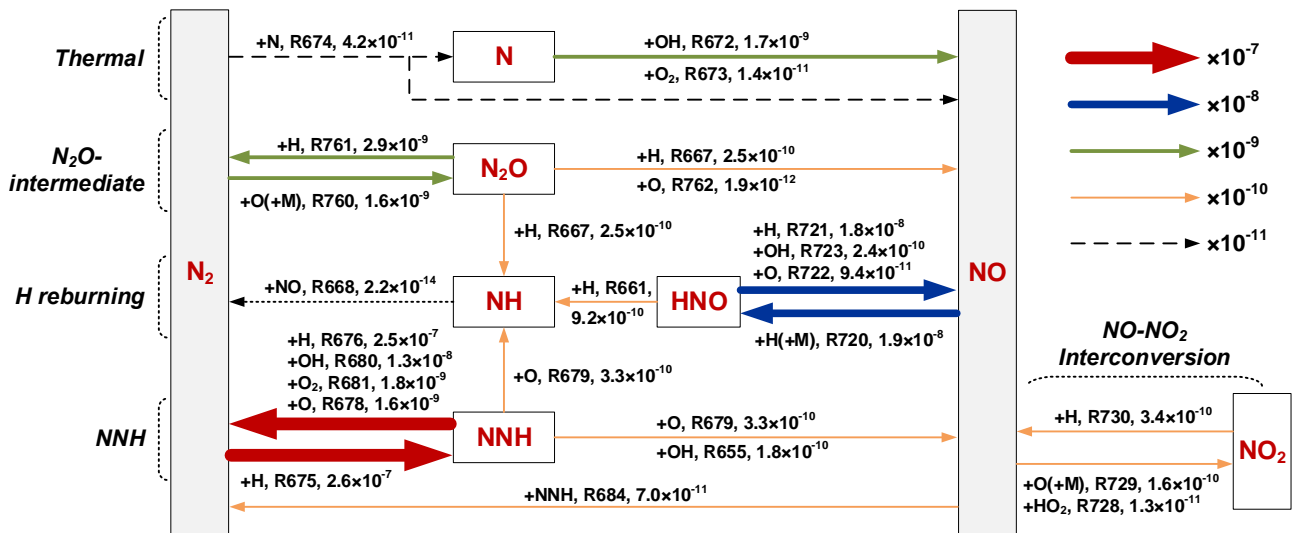
271 The JSR experimental data of NO as a function of temperature from 700 to 1150 K during the
272 oxidation of a 1% H₂/O₂/N₂/NO mixture doped with 235 ppm NO at $\varphi=1.5$ [61] are compared in Figure
273 4(f) to evaluate NO reduction by H radicals. If the H reburning initiation reaction is omitted from
274 Glarborg2018, NO reduction does not occur and NO almost remains at a constant value close to 235
275 ppm doped initially.

276 Based on the above analysis, it is concluded that the present NO sub-pathway analysis method
277 with Glarborg2018 can respectively predict NO formation via thermal, prompt, N₂O-intermediate, and
278 NNH pathways as well as NO reduction via CH_i and H reburning pathways reasonably well.

279 **4. Results and discussion**

280 **4.1. Quantitative NO reaction path diagram analysis**

281 The quantitative NO reaction pathway diagram analysis is first performed with Glarborg2018 to
 282 get an overall recognition of the NO chemistry kinetic for pure hydrogen MILD combustion. Figure 5
 283 shows the pathways forming and reducing NO in pure hydrogen MILD combustion at $X_{O_2} = 4\%$, $a_s =$
 284 100 s^{-1} , and $P = 1 \text{ atm}$, where the reaction rate of each pathway is obtained by integrating the net
 285 production or consumption rate over the separation distance between the fuel and oxidant nozzles and
 286 the channels with overall rates less than $1.0 \times 10^{-11} \text{ mol} \cdot \text{cm}^{-3} \cdot \text{s}^{-1}$ are omitted.



287

288 **Figure 5. Quantitative reaction path diagram showing NO chemistry in pure hydrogen MILD**
 289 **combustion at $X_{O_2} = 4\%$, $a_s = 100 \text{ s}^{-1}$, and $P = 1 \text{ atm}$ (Unit: $\text{mol} \cdot \text{cm}^{-3} \cdot \text{s}^{-1}$).**

290 As seen in Figure 5, during pure hydrogen MILD combustion, NO is formed mainly through the
 291 thermal, N₂O-intermediate, and NNH pathways, based on the initiation reactions by which N₂ is
 292 converted to N or other N-containing intermediate species. The thermal-NO mechanism [62], which
 293 proceeds via the pathway $\text{N}_2 \xrightarrow{+\text{O}} \text{N} \xrightarrow{+\text{O}_2, \text{OH}} \text{NO}$, controlled by a set of temperature-dependent channels:

294 $N_2+O\rightarrow NO$ (R674), $N+O_2\rightarrow NO$ (R673), and $N+OH\rightarrow NO$ (R672). Figure 5 reveals that the rate of
 295 production (ROP) of the initiation reaction $N+NO\rightleftharpoons N_2+O$ (R674) is lower due to the low reaction
 296 temperature. The N_2O -intermediate mechanism [64], mainly via the pathway $N_2 \xrightarrow{+O(+M)} N_2O \xrightarrow{+O, H} NO$,
 297 is initiated by the reaction $N_2+O\rightarrow N_2O$ (R760) and then the N_2O formed is partially converted to NO
 298 by combining H/O radicals via the channels $N_2O+H\rightarrow NO$ (R667) and $N_2O+O\rightarrow NO$ (R762). NO is
 299 also yielded via NNH, which is initiated by the reactions of N_2 with H radicals via $N_2+H\rightarrow NNH$
 300 (R675), and the NNH produced is further oxidized to NO with O radicals via $NNH+O\rightarrow NO$ (R679).
 301 In addition to the channel $NNH+O\rightarrow NO$ (R679), NNH is also consumed by OH to form NO via the
 302 backward reaction of $NH_2+NO\rightleftharpoons NNH+OH$ (R655). This is the NNH mechanism [65] mainly via the
 303 pathway $N_2 \xrightarrow{+H} NNH \xrightarrow{+O, OH} NO$.

304 The NO formed is also reduced by atomic hydrogen, which is initiated by the reaction
 305 $NO+H(+M)\rightleftharpoons HNO(+M)$ (R720) to yield the intermediate species HNO, and HNO is subsequently
 306 converted to NH via $HNO+H\rightarrow NH$ (R661), followed by reducing NO with NH via $NH+NO\rightarrow N_2$
 307 (R668). This is the mechanism of NO reburning with H radicals (i.e., H reburning), mainly via the
 308 pathway $NO \xrightarrow{+H} HNO \xrightarrow{+H} NH \xrightarrow{+NO} N_2$. Besides the above four mechanisms, the interconversion between
 309 NO and NO_2 also occurs through the following reactions $NO+HO_2\rightleftharpoons NO_2+OH$ (R728),
 310 $NO+O(+M)\rightleftharpoons NO_2(+M)$ (R729), and $NO_2+H\rightleftharpoons NO+OH$ (R730). Figure 5 reveals that almost all the
 311 reactions giving the production or consumption of NO involve reactions with one of O, H, and OH
 312 radicals, i.e., main agents of NO production/consumption, where O, H, and OH radicals are produced
 313 from the H_2/O_2 chain reactions $H+O_2\rightleftharpoons O+OH$ (R1), $O+H_2\rightleftharpoons OH+H$ (R3), $OH+H_2\rightleftharpoons H+H_2O$ (R4), and
 314 $OH+OH\rightleftharpoons O+H_2O$ (R5).

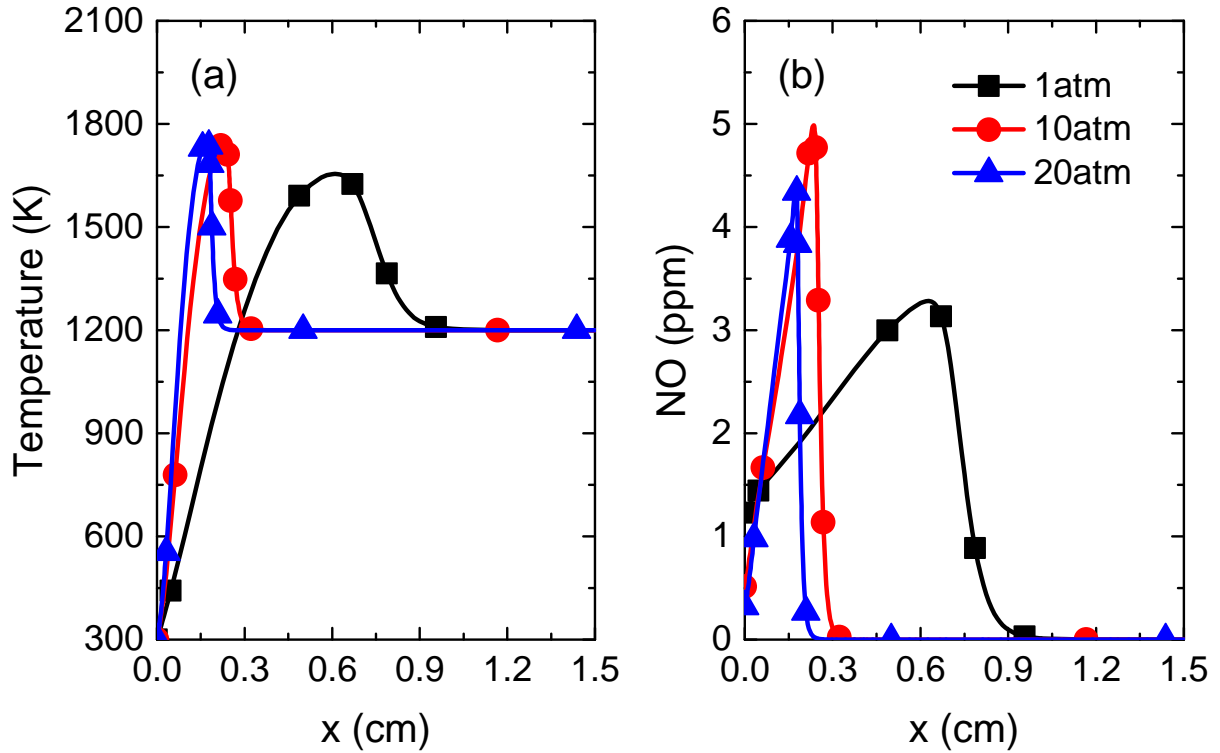
315 In general, for pure hydrogen MILD combustion, NO is formed mainly via the NNH (N_2
316 $\xrightarrow{+\text{H}} \text{NNH} \xrightarrow{+\text{O}, \text{OH}} \text{NO}$) and N_2O -intermediate ($\text{N}_2 \xrightarrow{+\text{O}(+\text{M})} \text{N}_2\text{O} \xrightarrow{+\text{O}, \text{H}} \text{NO}$) pathways and reduced via the H
317 reburning pathway ($\text{NO} \xrightarrow{+\text{H}} \text{HNO} \xrightarrow{+\text{H}} \text{NH} \xrightarrow{+\text{NO}} \text{N}_2$), and the thermal-NO pathway is less active due to low
318 combustion temperatures. The prompt-NO mechanism [66] is disabled and the classical NO reburning
319 mechanism [67] with hydrocarbon fragments is ineffective, due to the absence of hydrocarbon species.

320 4.2. Pressure effects

321 In this section, the effect of pressure from 1 to 25 atm (covering the operating pressure range of
322 typical E-class and state-of-the-art H/J-class heavy-duty gas turbines [41, 42]) on NO formation and
323 reduction pathways during pure hydrogen MILD combustion is characterized at $X_{\text{O}_2}=4\%$, $T_0=1200$
324 K, and $a_s=100 \text{ s}^{-1}$, namely Series 1 in Table 2.

325 4.2.1. Opposed-flow diffusion reactive structures

326 Figure 6 shows the profiles of temperature and NO in opposed-flow pure hydrogen flames under
327 MILD conditions. At higher pressure, the reacting flow structure moves towards the fuel side and
328 becomes thinner (see Figure 6(a)), thus causing a decrease in the width of the NO profile (see Figure
329 6(b)). Since the thickness of diffusion flames is of the order of $(D/a_s)^{1/2}$ [68] and the mixture
330 diffusion coefficient (D) is inversely proportional to pressure, the flame thickness is reduced at high
331 pressure. Besides, the peak temperature increases appreciably from 1655 to 1743 K with the pressure
332 from 1 to 10 atm, due to higher reaction intensity. Above 10 atm, the temperature increase is not as
333 significant and the peak temperature tends to level off with the pressure.



334

335 **Figure 6. Temperature and NO profiles in pure hydrogen MILD combustion at 1, 10, and 20**

336

atm.

337

As presented in Figure 6(b), pure hydrogen MILD combustion yields a single-digit NO peak at

338

all pressures. As the pressure rises from 1 to 25 atm, the peak NO mole fraction is increased first and

339

then reduced, following the opposite trend as the peak temperature at high pressure, which implies that

340

NO production is dominated by other mechanisms rather than the thermal-NO mechanism.

341

4.2.2. NO formation and reduction pathways

342

To grasp the pressure effects on NO chemistry, NO formation and destruction via different routes

343

are separately characterized in Figure 7, where the profiles of the NO formed via thermal, NNH, and

344

N_2O -intermediate pathways as well as the NO reduced via H reburning pathway are plotted versus the

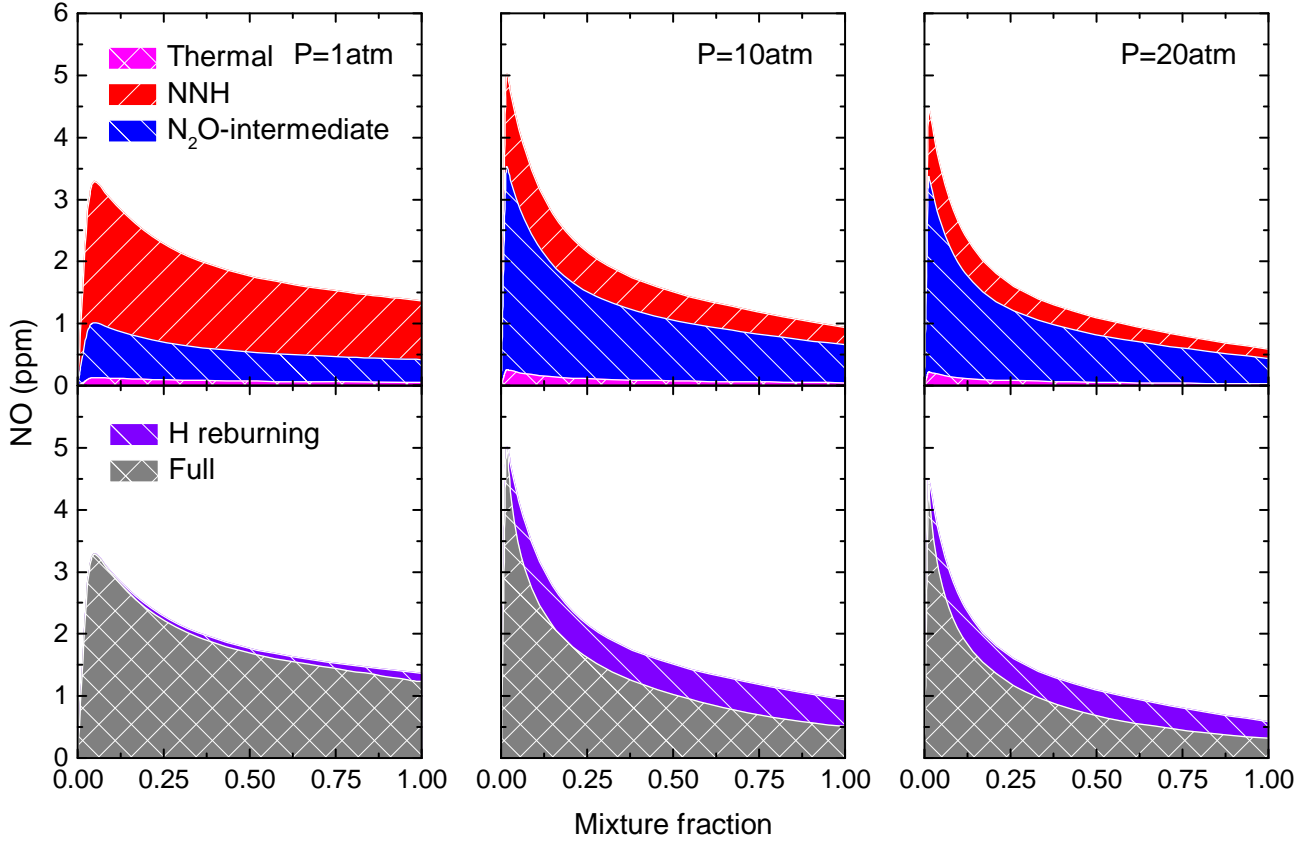
345

mixture fraction. Regardless of the pressure, the NO mole fraction increases first and then decreases

346

with the mixture fraction from 0 to 1, and the NO formed via all pathways reaches its peak close to the

347 flame front. Although the peak NO mole fraction exhibits a non-monotonous variation with the
348 pressure, increasing the pressure leads to a monotonous reduction in the net NO mole fraction (gray
349 color) on the fuel-rich side of the flame sheet. This occurs perhaps because of the reduction in the NO
350 formed via NNH, and/or the enhancement of NO reduction by H atoms. At 1 atm, NO is formed mainly
351 via the NNH and N₂O-intermediate routes, which matches the observation in a well-stirred reactor [40],
352 and the thermal-NO route is less important due to the low reaction temperature. As the pressure
353 increases, the amount of the NO contributed by the N₂O-intermediate route rises first and then drops
354 while that contributed by the NNH route reduces monotonously. The thermal-NO route is enhanced at
355 high pressure but such an increase is limited owing to its strong temperature dependence. In addition,
356 NO reduction by H radicals is much more noticeable on the fuel-rich side, due to its higher
357 effectiveness of NO reduction under reducing conditions [40, 69, 70], and it tends to become more
358 appreciable at high pressure.



359

360

Figure 7. Profiles of the NO formed and reduced via different pathways against mixture fraction in pure hydrogen MILD combustion at 1, 10, and 20 atm.

361

362

The global NO emission index (EINO) is used to further characterize the absolute and relative

363

amount of the NO formed or destroyed over a wide range of pressures, which is defined as [71]:

$$\text{EINO (g-NO/kg-Fuel)} = \frac{\int_0^L \dot{\omega}_{\text{NO}} M_{\text{NO}} dx}{-\int_0^L \dot{\omega}_{\text{Fuel}} M_{\text{Fuel}} dx} = \frac{\int_0^L \dot{\omega}_{\text{NO}} M_{\text{NO}} dx}{-\int_0^L \dot{\omega}_{\text{H}_2} M_{\text{H}_2} dx} \quad (2)$$

364

Here, M_i is the molecular weight, $\dot{\omega}$ the rate of production or consumption, L the separation

365

distance between the two nozzles, and x the axial coordinate.

366

Figure 8 shows the variation of absolute and relative amounts of the EINO contributed by the

367

thermal, NNH, N_2O -intermediate, and H reburning routes with the pressure from 1 to 25 atm. As

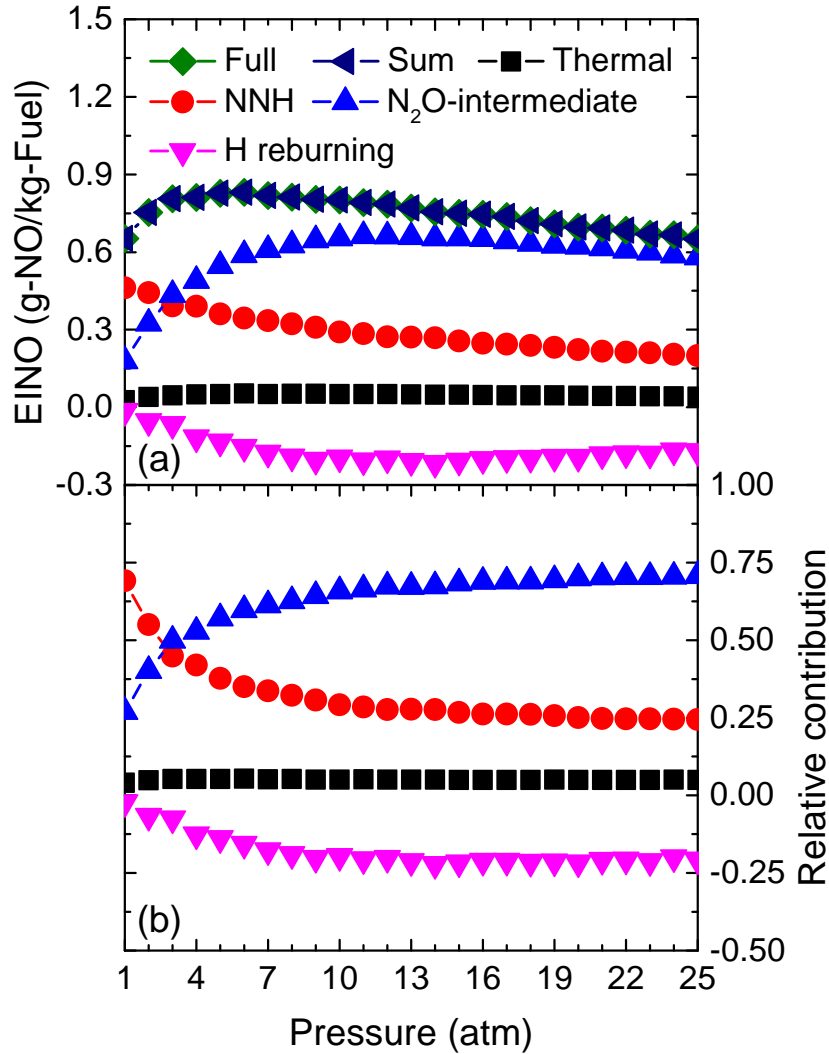
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plotted in Figure 8(a), the sum of the EINO produced via all the sub-pathways (termed Sum) almost

369

agrees with that of the full mechanism (termed Full), which demonstrates that the present NO sub-

370 pathway analysis method is reliable with a good decoupling effect among NO sub-mechanisms. [Figure](#)
371 [8\(a\)](#) reveals that the total EINO presents an increasing trend with the pressure up to about 6 atm due
372 to more NO formed via N₂O-intermediate, followed by a decreasing trend with further increasing
373 pressure to 25 atm, which is mainly attributed to lower NO formation via NNH and higher NO
374 reduction by H radicals. Somewhat differently, Shi et al. [\[33\]](#) reported the total EINO presents a
375 monotonic decreasing trend with pressure from 1 to 20 atm in syngas MILD combustion using the
376 NO_x sub-model from GRI-Mech 2.11, due to the decrease in the NO formed via NNH higher than the
377 increase via N₂O. Such a difference may be caused by the use of different NO_x sub-models. Indeed,
378 the low formation rate of the NNH pathway determined by Glarborg2018 refers to the study of
379 Klippenstein et al. [\[72\]](#), who reported that the importance of the NNH mechanism in forming NO may
380 be overestimated in the kinetic reaction mechanism developed earlier. Overall, the underlying reason
381 for a rise and then a drop in EINO with pressure may be the synergistic interaction between the total
382 NO production rate and the reaction zone size. At high pressure, the NO production rate is promoted,
383 while the reaction zone is concentrated ([Figure 6\(a\)](#)). When the pressure rises slightly, the reduction of
384 the reaction zone is not very significant, which generally leads to a rise in EINO when the pressure
385 starts to increase. However, the considerable reduction of the reaction zone when the pressure increases
386 significantly, to some extent, offsets the impact of the increase in the NO production rate, which causes
387 the drop in EINO at higher pressure.



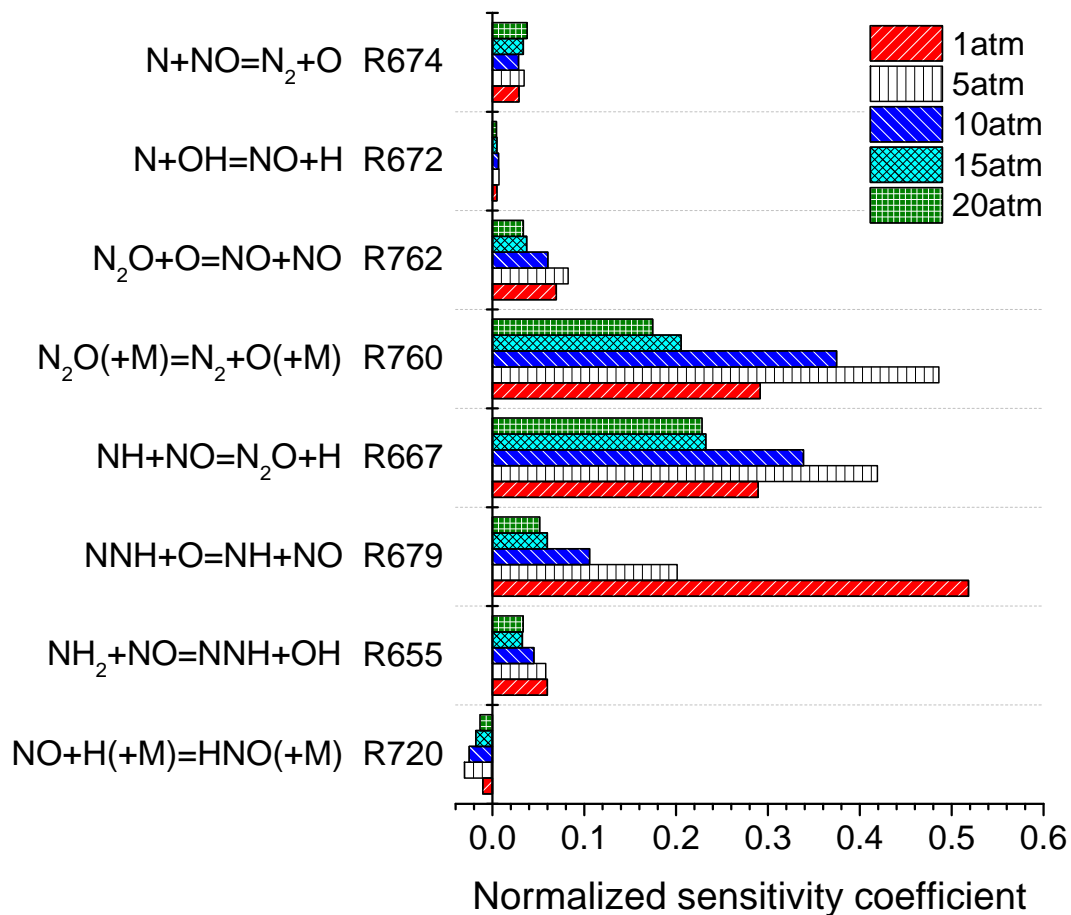
388

389 **Figure 8. NO formation and reduction characteristics in pure hydrogen MILD combustion at**
 390 **pressure from 1 to 25 atm.**

391 Another observation in Figure 8(a) is that the EINO value is comparable between 1 and 25 atm,
 392 which implies that higher pressure is favorable to the reduction of NO emission for pure hydrogen
 393 MILD combustion. It is recommended to operate at a higher pressure for minimizing NO emission
 394 under the premise of ensuring the realization of pure hydrogen MILD combustion.

395 Figure 8(b) further exhibits the relative contribution of these pathways to the total NO production
 396 at pressures of 1-25 atm. Sensitivity analysis is done to ascertain the important reactions responsible
 397 for NO formation and reduction, as displayed in Figure 9. It can be noticed that the NNH route mainly

398 via the channels $\text{NNH}+\text{O}/\text{OH}\rightarrow\text{NO}$, where the NNH radicals are solely produced by the channel N_2+H
399 (R675), controls the total NO production at atmospheric pressure, which contributes to 69% of the
400 total NO produced. This study is further extended to high pressure based on our recent research [40].
401 [Figure 9](#) reveals that as the pressure increases from 1 to 25 atm, the role of $\text{NNH}+\text{O}\rightleftharpoons\text{NH}+\text{NO}$ (R679)
402 and $\text{NH}_2+\text{NO}\rightleftharpoons\text{NNH}+\text{OH}$ (R655) in forming NO is weakened, causing the relative importance of the
403 NNH route to reduce from 69 to 24%. However, the importance of the N_2O -intermediate route via
404 $\text{N}_2\text{O}(+\text{M})\rightleftharpoons\text{N}_2+\text{O}(+\text{M})$ (R760), $\text{NH}+\text{NO}\rightleftharpoons\text{N}_2\text{O}+\text{H}$ (R667), and $\text{N}_2\text{O}+\text{O}\rightleftharpoons\text{NO}+\text{NO}$ (R762) increases.
405 With the pressure up to nearly 3 atm, the relative contribution of the NNH and N_2O -intermediate routes
406 on NO formation is comparable, and further increasing pressure leads to the transition of the
407 predominant NO formation pathway from NNH to N_2O ; at 25 atm, the contribution makes up 71% for
408 the N_2O -intermediate route. On the other hand, the NO reburning with H radicals, which acts mainly
409 via the pathway $\text{NO}\xrightarrow{+\text{H}}\text{HNO}\xrightarrow{+\text{H}}\text{NH}\xrightarrow{+\text{NO}}\text{N}_2$, has the potential to reduce 2-21% of the total NO
410 produced over a wide range of pressures from 1 to 25 atm, and it becomes increasingly important at
411 high pressure (see [Figure 8](#)), due to the higher sensitivity of the initiation step $\text{NO}+\text{H}(+\text{M})\rightleftharpoons\text{HNO}(+\text{M})$
412 (R720) for NO reduction.



413

414 **Figure 9. Sensitivity coefficient of the key NO reactions in pure hydrogen MILD combustion at**
 415 **different pressures.**

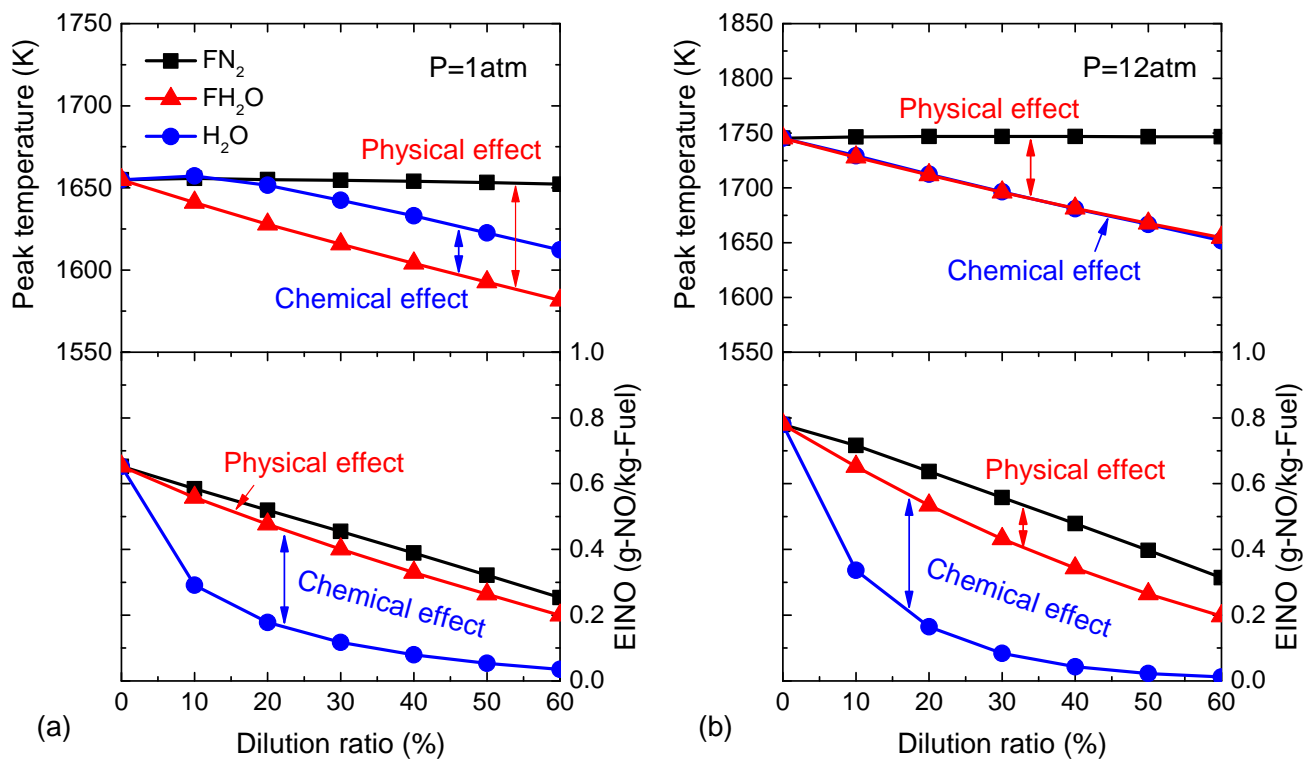
416 4.3. Physical and chemical effects of H₂O dilution

417 There is an ongoing need for NO reduction for pure hydrogen MILD combustion to achieve the
 418 goal of ultra-low and even near-zero NO emissions. Although H₂O dilution is known to be favorable
 419 for reducing NO emission [34, 53], it is still crucial to reveal how the reduction of NO proceeds during
 420 pure hydrogen MILD combustion if diluted by H₂O.

421 4.3.1. Characteristics of the NO formed and reduced via different pathways

422 Figure 10 shows the peak temperature and EINO during pure hydrogen MILD combustion diluted
 423 by 0-60%vol H₂O at 1 and 12 atm. As displayed in Figure 10, the peak temperature is reduced by less

424 than 100 K in the presence of 60%vol H₂O for both pressures, while a strong reduction of NO is
 425 observed with increasing H₂O dilution. The lower peak temperature in the presence of H₂O is largely
 426 caused by its physical effect at 1 and 12 atm, and such a physical effect is enhanced under high H₂O
 427 dilution conditions. However, regarding NO emission, the chemical effect of H₂O plays a stronger role
 428 in reducing the total EINO than the physical one over a wide range of X_{H_2O} from 0 to 60%.



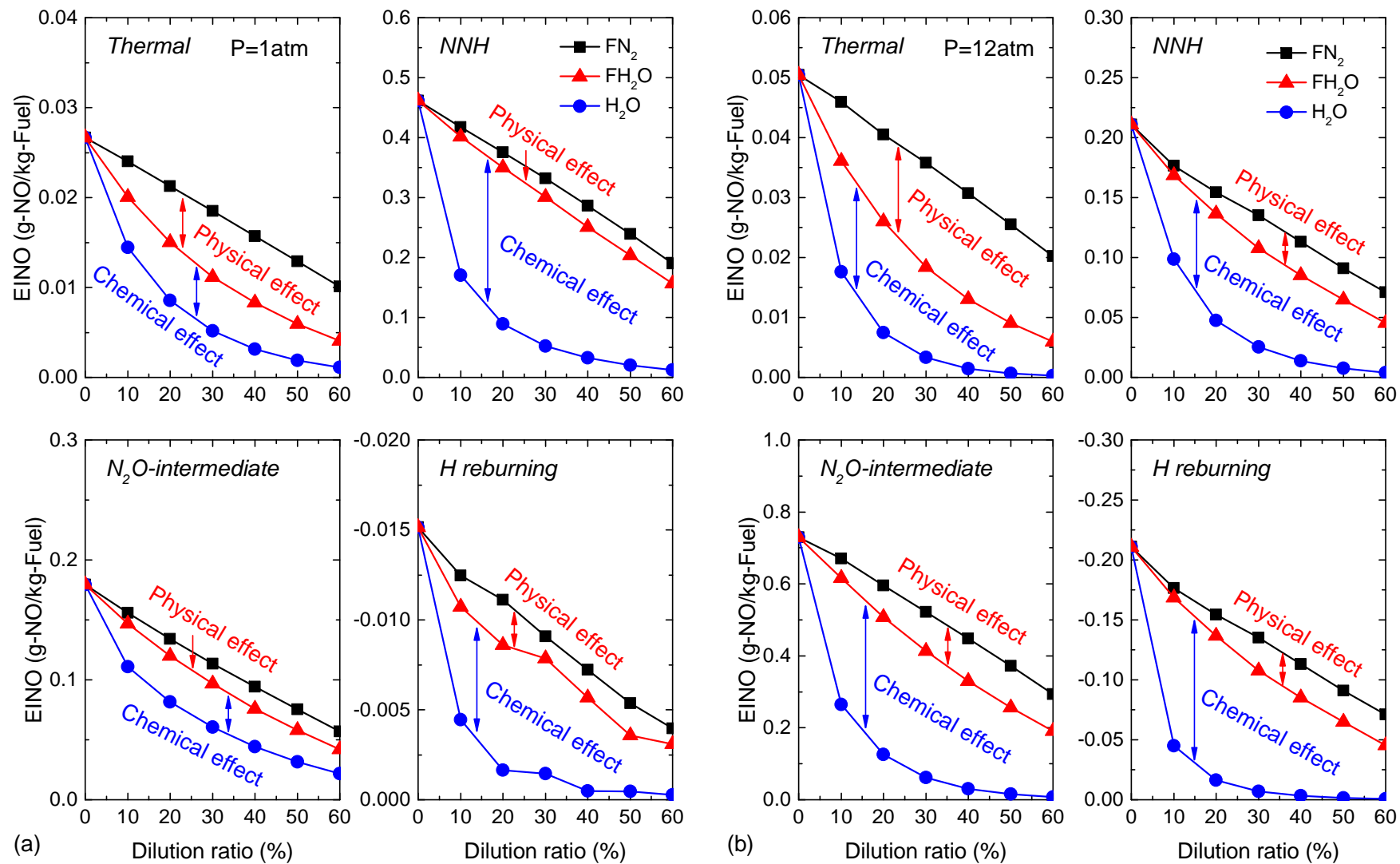
429

430 **Figure 10. Peak temperature and NO mole fraction in pure hydrogen MILD combustion with**

431 **H₂O dilution: (a) 1 atm, (b) 12 atm.**

432 The physical and chemical effects of H₂O on the NO formed and reduced via different pathways
 433 are further analyzed in Figure 11. All the routes for either NO formation or NO destruction are
 434 significantly blocked with H₂O addition at both pressures. H₂O dilution constrains NO production by
 435 reducing the formation of O, H, and OH radicals (the main agents of NO production, which is also
 436 attested in Figure 5) mainly through its chemical effect, see Figure 12(a). The chemical effect of H₂O

437 on the O radicals proceeds through the reactions $\text{H}+\text{O}_2(+\text{M})\rightleftharpoons\text{HO}_2(+\text{M})$ (R13) and $\text{OH}+\text{OH}\rightleftharpoons\text{O}+\text{H}_2\text{O}$
438 (R5), as well as on the H radicals proceeds through the reactions $\text{OH}+\text{H}_2\rightleftharpoons\text{H}+\text{H}_2\text{O}$ (R4) and $\text{O}+\text{H}_2\rightleftharpoons$
439 $\text{OH}+\text{H}$ (R3), further suppressing the rate of production and consumption of NO that comes from the
440 key steps $\text{NNH}+\text{O}$ (R679), $\text{N}_2\text{O}+\text{H}$ (R667), $\text{N}_2\text{O}+\text{O}$ (R762), and $\text{NO}+\text{H}$ (R720), as shown in [Figure](#)
441 [12\(b\)](#). And the effectiveness of the H₂O chemical role fades with H₂O addition up to 60%vol. Since
442 thermal NO is heavily dependent on temperature [\[62\]](#), H₂O dilution reduces the temperature caused
443 by higher specific heat capacity for H₂O relative to N₂, leading to the physical effect of H₂O mainly
444 responsible for the thermal NO reduction at high H₂O dilution through weakening the initiation
445 reaction $\text{N}_2+\text{O}\rightarrow\text{NO}$ (R674), as reflected by [Figure 12\(b\)](#).



446

447

Figure 11. Physical and chemical effects of H₂O on the NO formed and reduced via different pathways in pure hydrogen MILD

448

combustion: (a) 1 atm, (b) 12 atm.

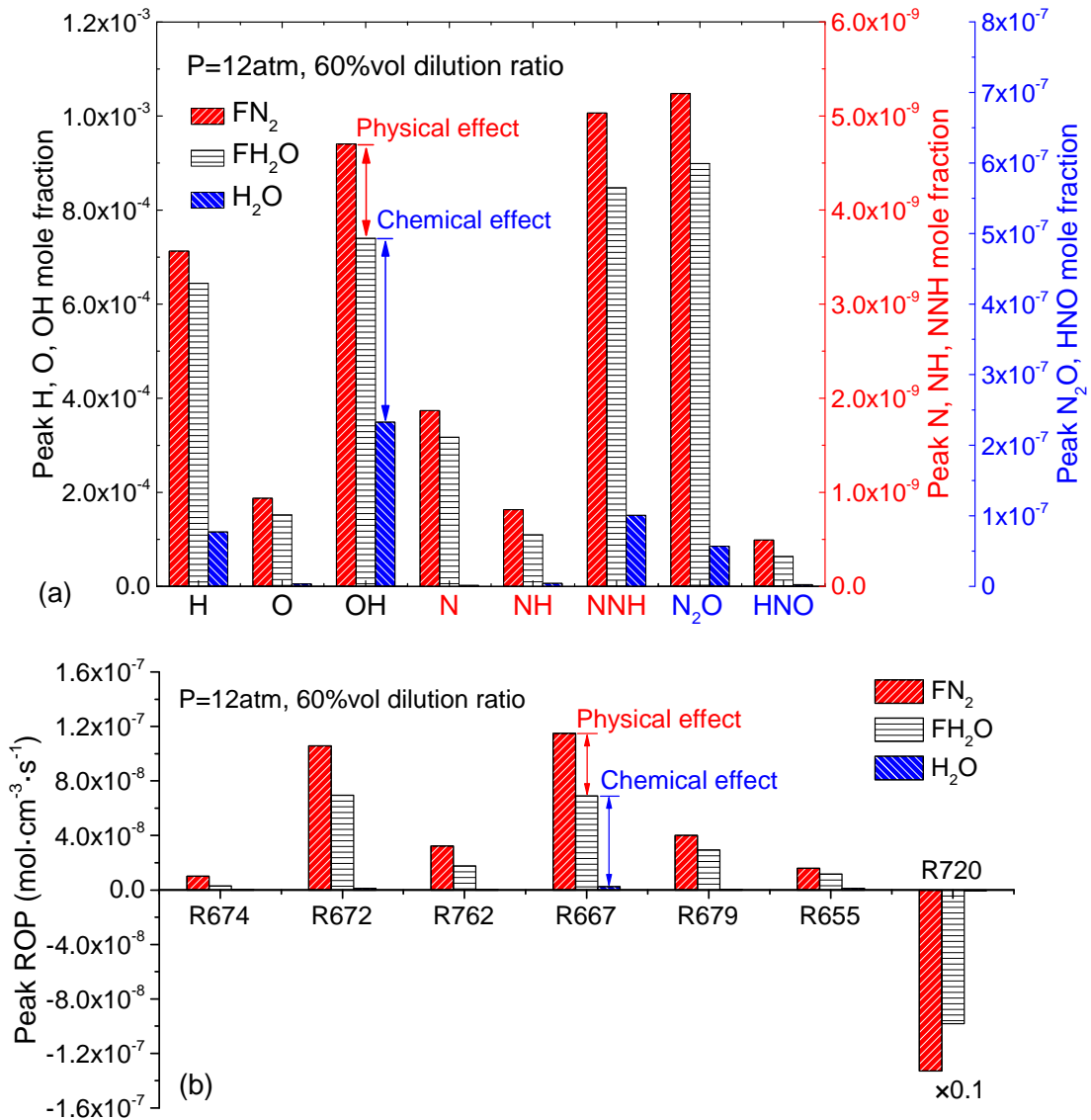


Figure 12. Physical and chemical effects of H_2O on the important NO-related (a) species and (b) reactions in pure hydrogen MILD combustion with 60%vol FN_2 , FH_2O , or H_2O dilution at 12 atm.

In summary, H_2O dilution can further reduce NO emission in pure hydrogen MILD combustion at atmospheric and high pressures, primarily because of its chemical effect to play a role of holdback on the production of the H, O, OH, N, NH, N_2O , NNH, and HNO radical pools and then to slower the NO production rate. It is recommended to increase burner-inlet H_2O injection or strengthen in-furnace recirculation of burnt gases (mainly H_2O) to achieve further NO control/reduction for pure hydrogen

MILD combustion in industrial applications.

4.3.2. Relative importance of the thermal, NNH, N₂O-intermediate, and H reburning pathways

Figure 13 further presents the contribution of different sub-routes to the total NO production with H₂O dilution at 1 and 12 atm, where NO is formed primarily via the following two routes: NNH and N₂O. At 1 atm, H₂O dilution reduces the contribution of the NO formed via NNH while increasing that via N₂O, and the N₂O-intermediate route surpasses the NNH route to become the dominant NO formation route when H₂O dilution exceeds about 25%vol. The NO sensitivity analysis in Figure 14 shows that, as H₂O is added from 0 to 60%vol, the importance of the NO contributed by NNH+O→NO (R679) decreases and that contributed by N₂O(+M)⇌N₂+O(+M) (R760) and NH+NO⇌N₂O+H (R667) increases, which clarifies the evolution of the NNH and N₂O-intermediate pathways with H₂O dilution.

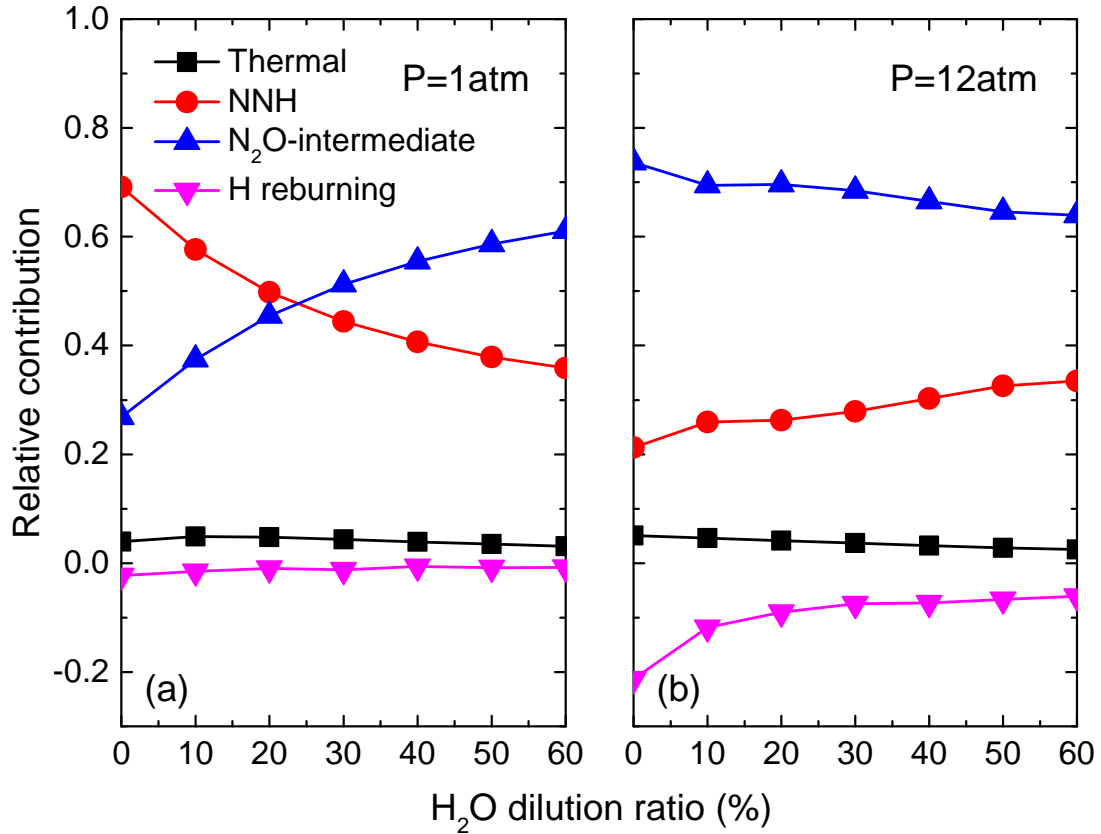


Figure 13. Variation of the contribution of different NO sub-pathways with H₂O dilution in pure hydrogen MILD combustion: (a) 1 atm, (b) 12 atm.

The response of the relative importance of different pathways to H₂O dilution at 12 atm follows a somewhat different trend at 1 atm, where the difference lies largely in that H₂O addition even up to 60%vol does not change the major NO formation pathway via N₂O at high pressure. At 12 atm, NO is formed mostly from the reaction of N₂O with H and O via $\text{N}_2\text{O} + \text{H} \rightarrow \text{NH} + \text{NO}$ (R667) and $\text{N}_2\text{O} + \text{O} \rightarrow \text{NO} + \text{NO}$ (R762), where N₂O is produced via the backward reaction of $\text{N}_2\text{O} (+\text{M}) \rightleftharpoons \text{N}_2 + \text{O} (+\text{M})$ (R760). The importance of these reactions in forming NO decreases if N₂ is replaced by H₂O. Therefore, the addition of H₂O weakens the effect of the N₂O-intermediate pathway, although it does not change the dominant role of the pathway via N₂O in NO formation. As for the NNH pathway, the channel $\text{NNH} + \text{OH} \rightarrow \text{NO}$ (R655) is more important than $\text{NNH} + \text{O} \rightarrow \text{NO}$ (R679) at high pressure. Despite lower

sensitivity for $\text{NNH}+\text{O}\rightarrow\text{NO}$ (R679) at high H_2O contents, H_2O dilution increases the sensitivity coefficient of $\text{NNH}+\text{OH}\rightarrow\text{NO}$ (R655), finally enhancing the importance of the NNH pathway with H_2O addition at high pressure. On the other hand, NO reduction by H atoms via $\text{NO}+\text{H}(+\text{M})\rightleftharpoons\text{HNO}(+\text{M})$ (R720) is enhanced at high pressure, accounting for 21% at 12 atm without H_2O dilution (see Figure 13), while its contribution is weakened by 71.4% up to 6% when with the replacement of N_2 by H_2O at 60%vol. As H_2O is added, the H radical concentration is lowered largely due to its chemical effect and then the role of the initiation channel $\text{NO}+\text{H}\rightarrow\text{HNO}$ (R720) is suppressed in NO decomposition.

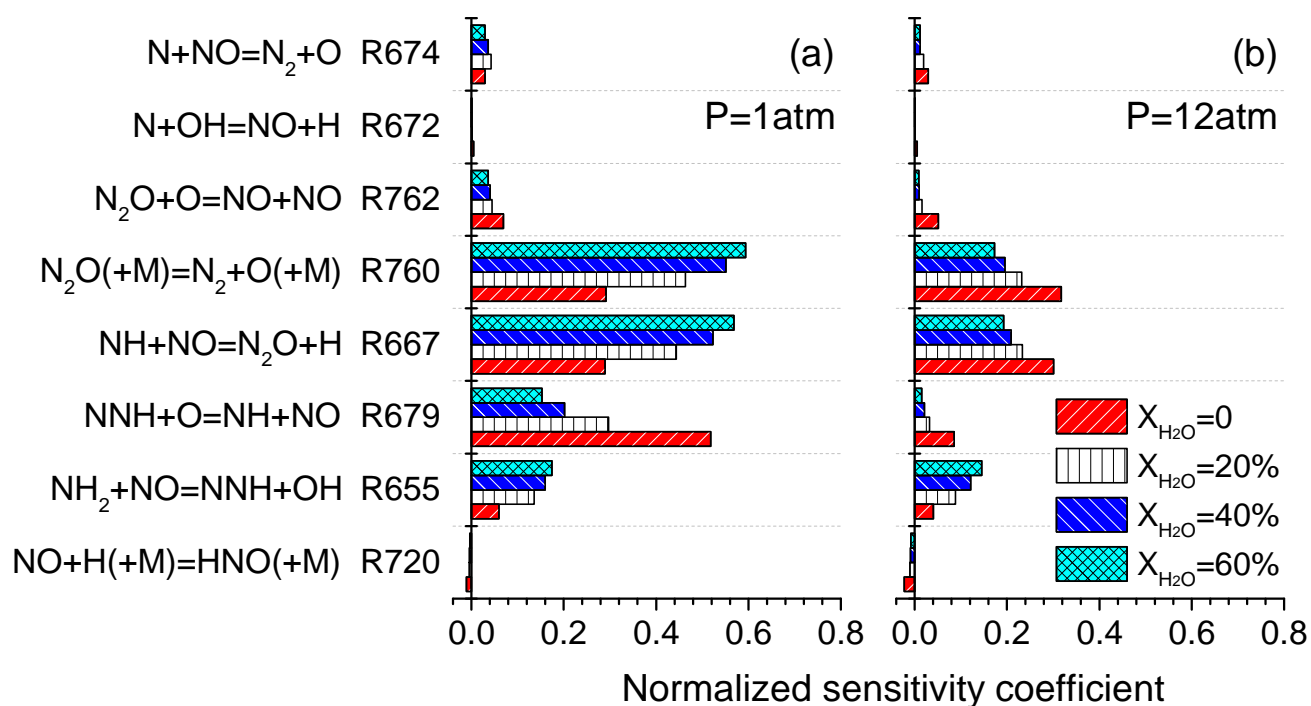


Figure 14. Sensitivity coefficient of the key NO reactions in pure hydrogen MILD combustion with H_2O dilution: (a) 1 atm, (b) 12 atm.

4.4. Evolution of the predominant NO forming or reducing pathway with pressure and H₂O dilution

Based on the above analysis, the major pathway of NO production or NO consumption is strongly dependent on pressure and H₂O dilution. Figure 15 further shows the evolution of the top contributor to NO formation as well as the importance of NO reduction by H radicals with pressure and H₂O dilution during pure hydrogen MILD combustion at $X_{O_2} = 4\%$, $T_0 = 1200$ K, $\phi = 1.0$, and $a_s = 100$ s⁻¹. In Figure 15(a), the NNH route is found to be the dominant NO formation one under a low percentage of H₂O dilution at low pressures (e.g., < 3 atm), while the N₂O-intermediate pathway is the top NO contributor at high H₂O dilution levels or/and high pressures. Figure 15(b) reveals that NO reburning with H radicals is effective to reduce NO, and its role becomes more significant at high pressures, constituting about 21% of the total NO at 25 atm, whereas weakened by 71.4% from 21 to 6% with H₂O addition from 0 to 60%vol at 12 atm. It is suggested that how to cut off the N₂O-intermediate pathway as the top NO contributor needs to be addressed if further NO emission reduction is required under high-pressure or/and H₂O-diluted conditions.

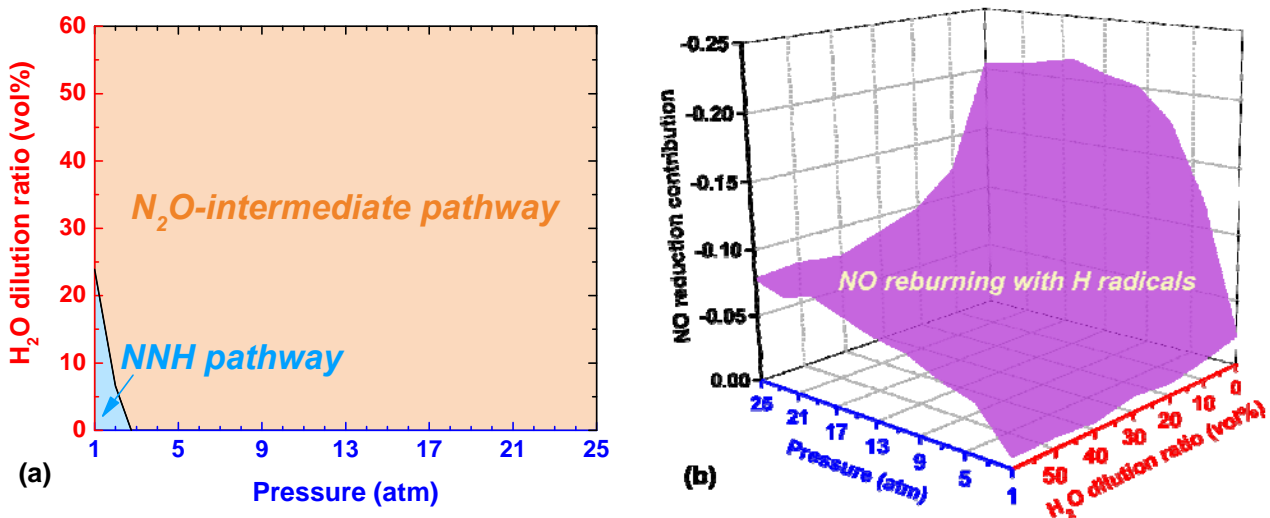


Figure 15. Evolution of the top contributor to (a) NO formation and (b) NO reduction with

pressure and H₂O dilution in pure hydrogen MILD combustion.

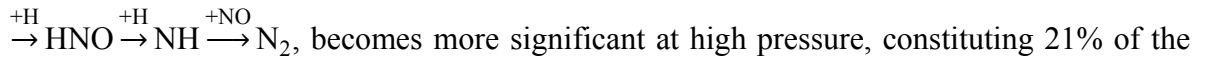
5. Conclusions

An opposed-flow diffusion flame model with Glarborg2018 is used to investigate NO reaction pathways in pure hydrogen MILD combustion. In particular, the present NO sub-pathway analysis method with Glarborg2018 for predicting thermal NO, prompt NO, NO formed via NNH and N₂O-intermediate pathways as well as NO reduced via CH_i and H reburning pathways is evaluated, and then the influence of pressure (1-25 atm) and H₂O dilution (0-60%vol) on NO formation and reduction via thermal, NNH, N₂O-intermediate, and H reburning pathways is analyzed, where the physical and chemical effects of H₂O are also identified. Important findings of the present study are given below.

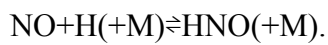
- (1) The present NO sub-pathway analysis method with Glarborg2018 can respectively predict thermal NO, prompt NO, NO formed via N₂O and NNH, and NO reduced via CH_i and H reburning pathways reasonably well.
- (2) The EINO increases its peak with the pressure up to about 6 atm due to more NO formed via N₂O, and then starts to descent as the pressure is further increased up to 25 atm, which is mainly attributed to less NO formation via NNH and more NO reduction by H radicals, ultimately causing the dominant NO formation route to change from NNH to N₂O at high pressure.
- (3) H₂O addition can achieve further NO emission reduction, which is primarily caused by the chemical effect of H₂O inhibiting the NNH and N₂O-intermediate pathways via the channels NNH+O/OH and N₂O+H/O to form NO. The dominant NO production route is changed from NNH to N₂O when H₂O dilution is larger than about 25%vol at atmospheric pressure, while

at high pressure, the N₂O-intermediate pathway is invariably the largest contributor to NO formation by H₂O dilution even up to 60%vol.

(4) NO reduction, which is initiated by reacting with H radicals mainly via the pathway



becomes more significant at high pressure, constituting 21% of the total NO produced at 25 atm, whereas its importance is decreased with H₂O dilution due to the chemical effect of H₂O to hinder H production and then to weaken the initiation channel



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